NAG Toolbox for MATLAB

f11gf

1 Purpose

fl1gf is the third in a suite of three functions for the iterative solution of a symmetric system of simultaneous linear equations (see Golub and Van Loan 1996). fl1gf returns information about the computations during an iteration and/or after this has been completed. The first function of the suite, fl1gd, is a setup function, the second function, fl1ge is the proper iterative solver.

These three functions are suitable for the solution of large sparse symmetric systems of equations.

2 Syntax

```
[itn, stplhs, stprhs, anorm, sigmax, its, sigerr, ifail] = f11gf(work,
'lwork', lwork)
```

3 Description

fl1gf returns information about the solution process. It can be called either during a monitoring step of fl1ge or after fl1ge has completed its tasks. Calling fl1gf at any other time will result in an error condition being raised.

For further information you should read the documentation for fl1gd and fl1ge.

4 References

Golub G H and Van Loan C F 1996 Matrix Computations (3rd Edition) Johns Hopkins University Press, Baltimore

5 Parameters

5.1 Compulsory Input Parameters

1: work(lwork) - double array

The workspace work as returned by fl1ge (see also Section 3 of the document for fl1ge).

5.2 Optional Input Parameters

1: lwork - int32 scalar

Default: The dimension of the array work.

Constraint: **lwork** \geq 120.

Note: although the minimum value of **lwork** ensures the correct functioning of fl1gf, a larger value is required by the iterative solver fl1ge (see also Section 5 of the document for fl1gd).

5.3 Input Parameters Omitted from the MATLAB Interface

None.

5.4 Output Parameters

1: itn – int32 scalar

The number of iterations carried out by fl1ge.

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2: stplhs – double scalar

The current value of the left-hand side of the termination criterion used by f11ge.

3: stprhs – double scalar

The current value of the right-hand side of the termination criterion used by fl1ge.

4: anorm – double scalar

The norm $||A||_1 = ||A||_{\infty}$ when either it has been supplied to fl1gd or it has been estimated by fl1ge (see also Sections 3 and 5 of the document for fl1gd). Otherwise, **anorm** = 0.0 is returned.

5: sigmax – double scalar

The current estimate of the largest singular value $\sigma_1(\bar{A})$ of the preconditioned iteration matrix $\bar{A} = E^{-1}AE^{-T}$, when either it has been supplied to fl1gd or it has been estimated by fl1ge (see also Sections 3 and 5 of the document for fl1gd). Note that if **its** < **itn** then **sigmax** contains the final estimate. If, on final exit from fl1ge, **its** = **itn**, then the estimation of $\sigma_1(\bar{A})$ may have not converged; in this case you should look at the value returned in **sigerr**. Otherwise, **sigmax** = 0.0 is returned.

6: its – int32 scalar

The number of iterations employed so far in the computation of the estimate of $\sigma_1(\bar{A})$, the largest singular value of the preconditioned matrix $\bar{A} = E^{-1}AE^{-T}$, when $\sigma_1(\bar{A})$ has been estimated by fl1ge using the bisection method (see also Sections 3, 5 and 8 of the document for fl1gd). Otherwise, **its** = 0 is returned.

7: sigerr – double scalar

If $\sigma_1(\bar{A})$ has been estimated by fl1ge using bisection,

$$\mathbf{sigerr} = \max\left(\frac{\left|\sigma_1^{(k)} - \sigma_1^{(k-1)}\right|}{\sigma_1^{(k)}}, \frac{\left|\sigma_1^{(k)} - \sigma_1^{(k-2)}\right|}{\sigma_1^{(k)}}\right),$$

where k = its denotes the iteration number. The estimation has converged if **sigerr** \leq **sigtol** where **sigtol** is an input parameter to fl1gd. Otherwise, **sigerr** = 0.0 is returned.

8: ifail – int32 scalar

0 unless the function detects an error (see Section 6).

6 Error Indicators and Warnings

Errors or warnings detected by the function:

ifail = -i

If **ifail** = -i, parameter i had an illegal value on entry. The parameters are numbered as follows:

1: itn, 2: stplhs, 3: stprhs, 4: anorm, 5: sigmax, 6: its, 7: sigerr, 8: work, 9: lwork, 10: ifail.

ifail = 1

fl1gf has been called out of sequence. For example, the last call to fl1ge did not return irevcm = 3 or 4.

7 Accuracy

Not applicable.

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8 Further Comments

None.

9 Example

```
nnz = int32(16);
a = zeros(10000,1);
a(1:16) = [4;
     1;
     5;
     2;
     2;
     3;
     -1;
     1;
     4;
     1;
     -2;
     3;
     2;
     -1;
     -2;
     5];
irow = zeros(10000,1,'int32');
irow(1:16) = [int32(1);
     int32(2);
     int32(2);
     int32(3);
     int32(4);
     int32(4);
     int32(5);
     int32(5);
     int32(5);
     int32(6);
     int32(6);
     int32(6);
     int32(7);
     int32(7);
     int32(7);
     int32(7)];
icol = zeros(10000,1,'int32');
icol(1:16) = [int32(1);
     int32(1);
     int32(2);
     int32(3);
     int32(2);
     int32(4);
     int32(1);
     int32(4);
     int32(5);
     int32(2);
     int32(5);
     int32(6);
     int32(1);
     int32(2);
     int32(3);
     int32(7)];
lfill = int32(0);
dtol = 0;
mic = 'N';
dscale = 0;
ipiv = zeros(7, 1, 'int32');
method = 'CG
precon = 'P';
n = int32(7);
tol = 1e-06;
```

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```
maxitn = int32(20);
anorm = 0;
sigmax = 0;
maxits = int32(7);
monit = int32(2);
irevcm = int32(0);
u = [0; 0; 0; 0; 0; 0; 0];
v = [15; 18; -8; 21; 11; 10; 29];
wgt = [0; 0; 0; 0; 0; 0; 0];
[a, irow, icol, ipiv, istr, nnzc, npivm, ifail] = ...
   fllja(nnz, a, irow, icol, lfill, dtol, mic, dscale, ipiv);
[lwreq, work, ifail] = ...
     f11gd(method, precon, n, tol, maxitn, anorm, sigmax, maxits, monit,
'sigcmp', 'S', 'norm_p', '1');
while (irevcm ~= 4)
  [irevcm, u, v, work, ifail] = f11ge(irevcm, u, v, wgt, work);
  if (irevcm == 1)
    [v, ifail] = f11xe(a(1:nnz), irow(1:nnz), icol(1:nnz), 'N', u);
    if (ifail = 0)
      irecvm = 6;
    end
  elseif (irevcm == 2)
    [v, ifail] = f11jb(a, irow, icol, ipiv, istr, 'N', u); if (ifail \tilde{} = 0)
     irecvm = 6;
    end
  elseif (irevcm == 3)
        [itn, stplhs, stprhs, anorm, sigmax, its, sigerr, ifail] =
f11qf(work);
    if (ifail ~= 0)
     irecvm = 6;
        fprintf('\nMonitoring at iteration number %d\nresidual norm:
14.4e\n', itn, stplhs);
   fprintf('\n
                 Solution Vector Residual Vector\n');
    for i = 1:n
      fprintf('%+16.4e %+16.4e\n', u(i), v(i));
  end
end
% Get information about the computation
[itn, stplhs, stprhs, anorm, sigmax, its, sigerr, ifail] = f11gf(work);
fprintf('\nNumber of iterations for convergence: %d\n', itn);
fprintf('Residual norm:
                                                    14.4e\n', stplhs);
fprintf('Right-hand side of termination criteria: %14.4e\n', stprhs);
fprintf('i-norm of matrix a:
                                                    %14.4e\n', anorm);
\texttt{fprintf('} \backslash \texttt{n}
              Solution Vector Residual Vector\n');
for i = 1:n
 fprintf('%+16.4e %+16.4e\n', u(i), v(i));
Monitoring at iteration number 2
residual norm:
                  1.9938e+00
   Solution Vector Residual Vector
     +9.6320e-01
                      -2.2960e-01
     +1.9934e+00
                      +2.2254e-01
     +3.0583e+00
                      +9.5827e-02
     +4.1453e+00
                      -2.5155e-01
     +4.8289e+00
                      -1.7160e-01
     +5.6630e+00
                      +6.7533e-01
     +7.1062e+00
                      -3.4737e-01
Monitoring at iteration number 4
residual norm: 6.6574e-03
```

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```
Solution Vector Residual Vector
                 -1.0551e-03
     +9.9940e-01
     +2.0011e+00
                    -2.4675e-03
    +3.0008e+00
                    -1.7116e-05
    +3.9996e+00
                    +4.4929e-05
     +4.9991e+00
                     +2.1359e-03
     +5.9993e+00
                     -8.7482e-04
     +7.0007e+00
                    +6.2045e-05
Number of iterations for convergence: 5
Residual norm:
                                            2.0428e-14
Right-hand side of termination criteria:
                                            3.9200e-04
i-norm of matrix a:
                                            1.0000e+01
   Solution Vector Residual Vector
+1.0000e+00
               +0.0000e+00
     +2.0000e+00
                     +0.0000e+00
     +3.0000e+00
                     -2.6645e-15
     +4.0000e+00
                     -3.5527e-15
    +5.0000e+00
                     -5.3291e-15
     +6.0000e+00
                     +1.7764e-15
                     +7.1054e-15
     +7.0000e+00
```

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